



FINAL JEE–MAIN EXAMINATION – SEPTEMBER, 2020

(On Thursday 03rd SEPTEMBER, 2020) TIME : 3 PM to 6 PM

MATHEMATICS

1. If the surface area of a cube is increasing at a rate of $3.6 \text{ cm}^2/\text{sec}$, retaining its shape; then the rate of change of its volume (in cm^3/sec), when the length of a side of the cube is 10 cm, is :

- (1) 9 (2) 18
(3) 10 (4) 20

Official Ans. by NTA (1)

2. If the value of the integral $\int_0^{1/2} \frac{x^2}{(1-x^2)^{3/2}} dx$ is $\frac{k}{6}$, then k is equal to :

- (1) $2\sqrt{3} - \pi$ (2) $3\sqrt{2} + \pi$
(3) $3\sqrt{2} - \pi$ (4) $2\sqrt{3} + \pi$

Official Ans. by NTA (1)

3. Let R_1 and R_2 be two relations defined as follows :

$$R_1 = \{(a, b) \in \mathbb{R}^2 : a^2 + b^2 \in \mathbb{Q}\} \text{ and}$$

$$R_2 = \{(a, b) \in \mathbb{R}^2 : a^2 + b^2 \notin \mathbb{Q}\},$$

where \mathbb{Q} is the set of all rational numbers. Then:

- (1) R_2 is transitive but R_1 is not transitive
(2) R_1 is transitive but R_2 is not transitive
(3) R_1 and R_2 are both transitive
(4) Neither R_1 nor R_2 is transitive

Official Ans. by NTA (4)

4. Let the latus rectum of the parabola $y^2 = 4x$ be the common chord to the circles C_1 and C_2 each of them having radius $2\sqrt{5}$. Then, the distance between the centres of the circles C_1 and C_2 is:

- (1) 8 (2) $4\sqrt{5}$
(3) 12 (4) $8\sqrt{5}$

Official Ans. by NTA (1)

TEST PAPER WITH ANSWER

5. If $\int \sin^{-1}\left(\sqrt{\frac{x}{1+x}}\right) dx = A(x)\tan^{-1}(\sqrt{x}) + B(x) + C$,

where C is a constant of integration, then the ordered pair $(A(x), B(x))$ can be :

- (1) $(x-1, \sqrt{x})$ (2) $(x+1, \sqrt{x})$
(3) $(x+1, -\sqrt{x})$ (4) $(x-1, -\sqrt{x})$

Official Ans. by NTA (3)

6. The probability that a randomly chosen 5-digit number is made from exactly two digits is :

- (1) $\frac{121}{10^4}$ (2) $\frac{150}{10^4}$
(3) $\frac{135}{10^4}$ (4) $\frac{134}{10^4}$

Official Ans. by NTA (3)

7. If a ΔABC has vertices $A(-1, 7)$, $B(-7, 1)$ and $C(5, -5)$, then its orthocentre has coordinates:

- (1) $(3, -3)$ (2) $\left(-\frac{3}{5}, \frac{3}{5}\right)$
(3) $(-3, 3)$ (4) $\left(\frac{3}{5}, -\frac{3}{5}\right)$

Official Ans. by NTA (3)

8. If z_1, z_2 are complex numbers such that $\text{Re}(z_1) = |z_1 - 1|$, $\text{Re}(z_2) = |z_2 - 1|$ and

$\arg(z_1 - z_2) = \frac{\pi}{6}$, then $\text{Im}(z_1 + z_2)$ is equal to:

- (1) $\frac{\sqrt{3}}{2}$ (2) $\frac{2}{\sqrt{3}}$
(3) $\frac{1}{\sqrt{3}}$ (4) $2\sqrt{3}$

Official Ans. by NTA (4)

9. The plane which bisects the line joining the points (4, -2, 3) and (2, 4, -1) at right angles also passes through the point :

- (1) (4, 0, -1) (2) (4, 0, 1)
(3) (0, 1, -1) (4) (0, -1, 1)

Official Ans. by NTA (1)

10. $\lim_{x \rightarrow a} \frac{(a+2x)^{\frac{1}{3}} - (3x)^{\frac{1}{3}}}{(3a+x)^{\frac{1}{3}} - (4x)^{\frac{1}{3}}} (a \neq 0)$ is equal to :

- (1) $\left(\frac{2}{3}\right)\left(\frac{2}{9}\right)^{\frac{1}{3}}$ (2) $\left(\frac{2}{3}\right)^{\frac{4}{3}}$
(3) $\left(\frac{2}{9}\right)^{\frac{4}{3}}$ (4) $\left(\frac{2}{9}\right)\left(\frac{2}{3}\right)^{\frac{1}{3}}$

Official Ans. by NTA (1)

11. Let A be a 3×3 matrix such that

$$\text{adj } A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 0 & 2 \\ 1 & -2 & -1 \end{bmatrix} \text{ and}$$

$$B = \text{adj}(\text{adj } A).$$

If $|A| = \lambda$ and $|(B^{-1})^T| = \mu$, then the ordered pair, $(|\lambda|, \mu)$ is equal to :

- (1) $\left(9, \frac{1}{9}\right)$ (2) $\left(9, \frac{1}{81}\right)$
(3) $\left(3, \frac{1}{81}\right)$ (4) (3, 81)

Official Ans. by NTA (3)

12. Suppose $f(x)$ is a polynomial of degree four, having critical points at -1, 0, 1. If $T = \{x \in \mathbb{R} | f(x) = f(0)\}$, then the sum of squares of all the elements of T is :

- (1) 6 (2) 8
(3) 4 (4) 2

Official Ans. by NTA (3)

13. Let $a, b, c \in \mathbb{R}$ be such that $a^2 + b^2 + c^2 = 1$.

$$\text{If } a \cos \theta = b \cos \left(\theta + \frac{2\pi}{3}\right) = c \cos \left(\theta + \frac{4\pi}{3}\right),$$

where $\theta = \frac{\pi}{9}$, then the angle between the

vectors $a\hat{i} + b\hat{j} + c\hat{k}$ and $b\hat{i} + c\hat{j} + a\hat{k}$ is :

- (1) $\frac{\pi}{2}$ (2) 0
(3) $\frac{\pi}{9}$ (4) $\frac{2\pi}{3}$

Official Ans. by NTA (1)

14. If the sum of the series

$$20 + 19\frac{3}{5} + 19\frac{1}{5} + 18\frac{4}{5} + \dots \text{ upto } n^{\text{th}} \text{ term is } 488$$

and the n^{th} term is negative, then :

- (1) n^{th} term is $-4\frac{2}{5}$ (2) $n = 41$
(3) n^{th} term is -4 (4) $n = 60$

Official Ans. by NTA (3)

15. Let x_i ($1 \leq i \leq 10$) be ten observations of a random variable X. If $\sum_{i=1}^{10} (x_i - p) = 3$ and

$$\sum_{i=1}^{10} (x_i - p)^2 = 9 \text{ where } 0 \neq p \in \mathbb{R}, \text{ then the}$$

standard deviation of these observations is :

- (1) $\sqrt{\frac{3}{5}}$ (2) $\frac{7}{10}$
(3) $\frac{9}{10}$ (4) $\frac{4}{5}$

Official Ans. by NTA (3)

16. If $x^3 dy + xy dx = x^2 dy + 2y dx$; $y(2) = e$ and $x > 1$, then $y(4)$ is equal to :

- (1) $\frac{3}{2} + \sqrt{e}$ (2) $\frac{3}{2}\sqrt{e}$
 (3) $\frac{1}{2} + \sqrt{e}$ (4) $\frac{\sqrt{e}}{2}$

Official Ans. by NTA (2)

17. Let e_1 and e_2 be the eccentricities of the ellipse,

$$\frac{x^2}{25} + \frac{y^2}{b^2} = 1 (b < 5) \quad \text{and the hyperbola,}$$

$$\frac{x^2}{16} - \frac{y^2}{b^2} = 1 \quad \text{respectively satisfying } e_1 e_2 = 1. \text{ If}$$

α and β are the distances between the foci of the ellipse and the foci of the hyperbola respectively, then the ordered pair (α, β) is equal to :

- (1) (8, 10) (2) (8, 12)
 (3) $\left(\frac{20}{3}, 12\right)$ (4) $\left(\frac{24}{5}, 10\right)$

Official Ans. by NTA (1)

18. The set of all real values of λ for which the quadratic equations,

$(\lambda^2 + 1)x^2 - 4\lambda x + 2 = 0$ always have exactly one root in the interval (0, 1) is :

- (1) (-3, -1) (2) (1, 3]
 (3) (0, 2) (4) (2, 4]

Official Ans. by NTA (2)

19. If the term independent of x in the expansion

of $\left(\frac{3}{2}x^2 - \frac{1}{3x}\right)^9$ is k , then $18k$ is equal to :

- (1) 9 (2) 11
 (3) 5 (4) 7

Official Ans. by NTA (4)

20. Let p, q, r be three statements such that the truth value of $(p \wedge q) \rightarrow (\sim q \vee r)$ is F. Then the truth values of p, q, r are respectively :

- (1) T, F, T (2) F, T, F
 (3) T, T, F (4) T, T, T

Official Ans. by NTA (3)

21. If m arithmetic means (A.Ms) and three geometric means (G.Ms) are inserted between 3 and 243 such that 4th A.M. is equal to 2nd G.M., then m is equal to _____.

Official Ans. by NTA (39)

22. If the tangent of the curve, $y = e^x$ at a point (c, e^c) and the normal to the parabola, $y^2 = 4x$ at the point (1, 2) intersect at the same point on the x -axis, then the value of c is _____.

Official Ans. by NTA (4)

23. Let a plane P contain two lines

$$\vec{r} = \hat{i} + \lambda(\hat{i} + \hat{j}), \lambda \in \mathbb{R} \text{ and}$$

$$\vec{r} = -\hat{j} + \mu(\hat{j} - \hat{k}), \mu \in \mathbb{R}$$

If $Q(\alpha, \beta, \gamma)$ is the foot of the perpendicular drawn from the point $M(1, 0, 1)$ to P , then $3(\alpha + \beta + \gamma)$ equals _____.

Official Ans. by NTA (5)

24. Let S be the set of all integer solutions, (x, y, z) , of the system of equations

$$x - 2y + 5z = 0$$

$$-2x + 4y + z = 0$$

$$-7x + 14y + 9z = 0$$

such that $15 \leq x^2 + y^2 + z^2 \leq 150$. Then, the number of elements in the set S is equal to _____.

Official Ans. by NTA (8)

25. The total number of 3-digit numbers, whose sum of digits is 10, is _____.

Official Ans. by NTA (54)