

# M1

Time: 3 Hours

Questions: 30

Max Marks: 100

## INSTRUCTIONS

1. Use of mobile phones, smartphones, tablets, calculators, programmable wrist watches or any other electronic devices is **STRICTLY PROHIBITED**. Only ordinary pens and pencils are allowed inside the examination hall.
2. The correction is done by machines through scanning. On the OMR Sheet, darken bubbles completely with a **black or blue ball pen**. Please **DO NOT use pencil or a gel pen**. Darken the bubbles completely, only after you are sure of your answer; else, erasing may lead to the OMR sheet getting damaged and the machine may not be able to read the answer.
3. The name, email address, and date of birth entered on the OMR sheet will be your login credentials for accessing your score.
4. Incompletely, incorrectly or carelessly filled information may disqualify your candidature.
5. Each question has a one or two digit number as answer. The first diagram below shows improper and proper way of darkening the bubbles with detailed instructions. The second diagram shows how to mark a 2-digit number and a 1-digit number.

**INSTRUCTIONS**

1. "Think before your ink".
2. Marking should be done with Blue/Black Ball Point Pen only.
3. Darken only one circle for each question as shown in Example Below.

WRONG METHODS	CORRECT METHOD
	

4. If more than one circle is darkened or if the response is marked in any other way as shown "WRONG" above, it shall be treated as wrong way of marking.
5. Make the marks only in the spaces provided.
6. Carefully tear off the duplicate copy of the OMR without tampering the Original.
7. Please do not make any stray marks on the answer sheet.

Q. 1	Q. 2
	

6. The answer you write on OMR sheet is irrelevant. The darkened bubble will be considered as your final answer.
7. Questions 1 to 10 carry 2 marks each; questions 11 to 20 carry 3 marks each; questions 21 to 30 carry 5 marks each.
8. All questions are compulsory.
9. There are no negative marks.
10. Do all rough work in the space provided below for it. You also have blank pages at the end of the question paper to continue with rough work.
11. After the exam, you may take away the Candidate's copy of the OMR sheet.
12. Preserve your copy of OMR sheet till the end of current olympiad season. You will need it later for verification purposes.
13. You may take away the question paper after the examination.

**Note:**

1.  $\gcd(a, \sqrt{b})$  denotes the greatest common divisor of integers  $a$  and  $b$ .
2. For a positive real number  $m$ ,  $\sqrt{m}$  denotes the positive square root of  $m$ . For example,  $\sqrt{4} = +2$ .
3. Unless otherwise stated all numbers are written in decimal notation.

## Questions

1. If 60% of a number  $x$  is 40, then what is  $x\%$  of 60?
2. Find the number of positive integers  $n$  less than or equal to 100, which are divisible by 3 but are not divisible by 2.
3. The area of an integer-sided rectangle is 20. What is the minimum possible value of its perimeter?
4. How many isosceles integer-sided triangles are there with perimeter 23?
5. How many 3-digit numbers  $\overline{abc}$  in base 10 are there with  $a \neq 0$  and  $c = a + b$ ?

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Space for rough work

6. The age of a person (in years) in 2025 is a perfect square. His age (in years) was also a perfect square in 2012. His age (in years) will be a perfect cube  $m$  years after 2025. Determine the smallest value of  $m$ .
7. The sum of two real numbers is a positive integer  $n$  and the sum of their squares is  $n + 1012$ . Find the maximum possible value of  $n$ .
8. A quadrilateral has four vertices  $A, B, C, D$ . We want to colour each vertex in one of the four colours red, blue, green or yellow, so that every side of the quadrilateral and the diagonal  $AC$  have end points of different colours. In how many ways can we do this?
9. Four sides and a diagonal of a quadrilateral are of lengths 10, 20, 28, 50, 75, not necessarily in that order. Which amongst them is the only possible length of the diagonal?

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Space for rough work

10. The height and the base radius of a closed right circular cylinder are positive integers and its total surface area is numerically equal to its volume. If its volume is  $k\pi$  where  $k$  is a positive integer, what is the smallest possible value of  $k$ ?
11. Consider a fraction  $\frac{a}{b} \neq \frac{3}{4}$ , where  $a, b$  are positive integers with  $\gcd(a, b) = 1$  and  $b \leq 15$ . If this fraction is chosen closest to  $\frac{3}{4}$  amongst all such fractions, then what is the value of  $a + b$ ?
12. Consider five-digit positive integers of the form  $\overline{abcab}$  that are divisible by the two digit number  $\overline{ab}$  but not divisible by 13. What is the largest possible sum of the digits of such a number?

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Space for rough work

13. Three sides of a quadrilateral are  $a = 4\sqrt{3}$ ,  $b = 9$  and  $c = \sqrt{3}$ . The sides  $a$  and  $b$  enclose an angle of  $30^\circ$ , and the sides  $b$  and  $c$  enclose an angle of  $90^\circ$ . If the acute angle between the diagonals is  $x^\circ$ , what is the value of  $x$ ?
14. A function  $f$  is defined on the set of integers such that for any two integers  $m$  and  $n$ ,

$$f(mn + 1) = f(m)f(n) - f(n) - m + 2$$

holds and  $f(0) = 1$ . Determine the largest positive integer  $N$  such that  $\sum_{k=1}^N f(k) < 100$ .

15. There are six coupons numbered 1 to 6 and six envelopes, also numbered 1 to 6. The first two coupons are placed together in any one envelope. Similarly, the third and the fourth are placed together in a different envelope, and the last two are placed together in yet another different envelope. How many ways can this be done if no coupon is placed in the envelope having the same number as the coupon?

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Space for rough work

16. Let  $f(x)$  and  $g(x)$  be two polynomials of degree 2 such that

$$\frac{f(-2)}{g(-2)} = \frac{f(3)}{g(3)} = 4.$$

If  $g(5) = 2$ ,  $f(7) = 12$ ,  $g(7) = -6$ , what is the value of  $f(5)$ ?

17.  $MTAI$  is a parallelogram of area  $\frac{40}{41}$  square units such that  $MI = 1/MT$ . If  $d$  is the least possible length of the diagonal  $MA$ , and  $d^2 = \frac{a}{b}$ , where  $a, b$  are positive integers with  $\gcd(a, b) = 1$ , find  $|a - b|$ .
18. Let  $N$  be the number of nine-digit integers that can be obtained by permuting the digits of 223334444 and which have at least one 3 to the right of the right-most occurrence of 4. What is the remainder when  $N$  is divided by 100?

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Space for rough work

19. In triangle  $ABC$ ,  $\angle B = 90^\circ$ ,  $AB = 1$  and  $BC = 2$ . On the side  $BC$  there are two points  $D$  and  $E$  such that  $E$  lies between  $C$  and  $D$  and  $DEFG$  is a square, where  $F$  lies on  $AC$  and  $G$  lies on the circle through  $B$  with centre  $A$ . If the area of  $DEFG$  is  $\frac{m}{n}$  where  $m$  and  $n$  are positive integers with  $\gcd(m, n) = 1$ , what is the value of  $m + n$ ?

20. Let  $f$  be the function defined by

$$f(n) = \text{remainder when } n^n \text{ is divided by } 7,$$

for all positive integers  $n$ . Find the smallest positive integer  $T$  such that  $f(n+T) = f(n)$  for all positive integers  $n$ .

21. For some real numbers  $m, n$  and a positive integer  $a$ , the list  $(a+1)n^2, m^2, a(n+1)^2$  consists of three consecutive integers written in increasing order. What is the largest possible value of  $m^2$ ?

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Space for rough work

22. There are  $m$  blue marbles and  $n$  red marbles on a table. Armaan and Babita play a game by taking turns. In each turn the player has to pick a marble of the colour of his/her choice. Armaan starts first, and the player who picks the last red marble wins. For how many choices of  $(m, n)$  with  $1 \leq m, n \leq 11$  can Armaan force a win?
23. Let  $ABCD$  be a rectangle and let  $M, N$  be points lying on sides  $AB$  and  $BC$ , respectively. Assume that  $MC = CD$  and  $MD = MN$ , and that points  $C, D, M, N$  lie on a circle. If  $(AB/BC)^2 = m/n$  where  $m$  and  $n$  are positive integers with  $\gcd(m, n) = 1$ , what is the value of  $m + n$ ?
24. Let  $P(x) = x^{2025}$ ,  $Q(x) = x^4 + x^3 + 2x^2 + x + 1$ . Let  $R(x)$  be the polynomial remainder when the polynomial  $P(x)$  is divided by the polynomial  $Q(x)$ . Find  $R(3)$ .

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Space for rough work

25. For how many numbers  $n$  in the set  $\{1, 2, 3, \dots, 37\}$  can we split the  $2n$  numbers  $1, 2, \dots, 2n$  into  $n$  pairs  $\{a_i, b_i\}$ ,  $1 \leq i \leq n$ , such that  $\prod_{i=1}^n (a_i + b_i)$  is a square?

26. Consider a sequence of real numbers of finite length. Consecutive four term averages of this sequence are strictly increasing, but consecutive seven term averages are strictly decreasing. What is the maximum possible length of such a sequence?

27. Find the number of ordered triples  $(a, b, c)$  of positive integers such that  $1 \leq a, b, c \leq 50$  which satisfy the relation

$$\frac{\text{lcm}(a, c) + \text{lcm}(b, c)}{a + b} = \frac{26c}{27}.$$

Here, by  $\text{lcm}(x, y)$  we mean the LCM, that is, least common multiple of  $x$  and  $y$ .

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Space for rough work

28. Assume  $a$  is a positive integer which is not a perfect square. Let  $x, y$  be non-negative integers such that  $\sqrt{x - \sqrt{x + a}} = \sqrt{a} - y$ . What is the largest possible value of  $a$  such that  $a < 100$ ?
29. A regular polygon with  $n \geq 5$  vertices is said to be colourful if it is possible to colour the vertices using at most 6 colours such that each vertex is coloured with exactly one colour, and such that any 5 consecutive vertices have different colours. Find the largest number  $n$  for which a regular polygon with  $n$  vertices is **not** colourful.
30. Let  $S$  be a circle of radius 10 with centre  $O$ . Suppose  $S_1$  and  $S_2$  are two circles which touch  $S$  internally and intersect each other at two distinct points  $A$  and  $B$ . If  $\angle OAB = 90^\circ$  what is the sum of the radii of  $S_1$  and  $S_2$ ?

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Space for rough work

# Indian Olympiad Qualifier in Mathematics 2025

September 7, 2025

## Provisional Answer Key

	Set M1	Set M2	Set M3	Set M4		Set M1	Set M2	Set M3	Set M4
Q1	40	40	40	40	Q16	22	29	22	22
Q2	17	17	17	17	Q17	23	22	29	29
Q3	18	18	18	18	Q18	40	23	42	23
Q4	06	06	06	06	Q19	29	42	23	40
Q5	45	45	45	45	Q20	42	40	40	42
Q6	15	28	15	54	Q21	49	66	03	53
Q7	46	15	28	48	Q22	66	49	36	03
Q8	48	48	54	46	Q23	03	53	49	36
Q9	28	54	48	28	Q24	53	03	66	66
Q10	54	46	46	15	Q25	36	36	53	49
Q11	61	61	40	40	Q26	10	19	10	10
Q12	33	60	60	33	Q27	40	10	19	19
Q13	60	33	33	12	Q28	91	10	40	40
Q14	12	12	12	61	Q29	19	40	10	10
Q15	40	40	61	60	Q30	10	91	91	91

## Challenges

- Note: in above M1 = Set A, M2 = Set B, M3 = Set C and M4 =Set D.
- All challenges to the answer key above should be submitted through the following form <https://forms.gle/iXhkUvYCzZ4L7Dq89>.
- Last date for a challenge is **September 10th 2025**. Challenges received after this date will not be entertained.
- Challenges received through any other channel, including email, will NOT be entertained.